#### Accept this Paper

(Economic Theory Seminar, UK, May 2023)

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# Princeton offers admission to 5.5 percent of Class of 2022 applicants

by Office of Communications

March 28, 2018, 4 p.m.

# Selectivity as Excellence

Motivation

- Colleges advertise "selectivity"
- ▶ U.S. News and World Report college rankings puts 12.5% weight on selectivity
- ► The Princeton Review weights it as one of seven factors
- "Columbia Drops From #2 to #18 on University Rankings As School Officials Admit to Misleading Data" (09/12/22)
- Intuition: Since rejection rates are the de facto prices of better schools, better colleges should have higher rejection rates!

# PRINCET NIAN

Princeton University accepts 0.00% of applicants to Class of 2027

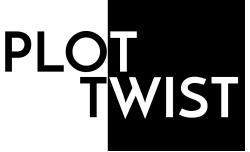


Motivation

- ▶ Should the best colleges have the highest rejection rates?
- Should the best journals have the highest rejection rates?
- Better journals have higher standards, but get better papers.
- Which effect should dominate?

#### Goal: Is Selectivity Excellence?

- Should the best colleges have the highest rejection rates?
- Should the best journals have the highest rejection rates?
- ▶ Better journals have higher standards, but get better papers.
- Which effect should dominate?



- ► We show that selectivity *robustly fails* at elite journals
- ▶ We leave the harder college problem open
  - has initial college portfolio choice, and final student choice
  - Lately, early admissions also complicates the college problem

#### Journal / College Quality is Endogenous

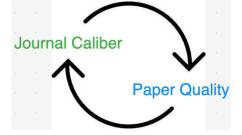
- ▶ There are no absolutely good or bad colleges or journals
  - Alternatively, college qualities are fixed (maybe by faculty) as is their student capacity
  - New journals face this problem all the time
  - Problem: Bad elite colleges can maintain high standards by shrinking enrollment [Chade, Lewis, and Smith (2014) "Student Portfolios and the College Admissions Problem"]
- ► For the purposes of valuing a college or journal:
  - ► A college is only as good as its students.
  - A journal is only as good as its papers

#### Matching as an Implicit Market

- Broad topic: Matching with incomplete information.
  - Asymmetry: journal qualities are known, paper qualities not
  - ► Complete information: use the deferred acceptance algorithm
- ▶ Journal Acceptance / College Admissions as Implicit Markets
  - ▶ Most elite journal money application fees are roughly similar
  - Acceptance bars and admission standards perform the allocation role of prices, and they adjust (highest for best journals and colleges)
  - ► This paper seeks to understand this market

#### Steady State Story

- ► All players negligible ⇒ games where journals move first then authors, or all act at once, have identical Bayes Nash equilibria
- Step 1 An endogenous capacity pool of journals indexed by caliber publicize and commit to standards
- Step 2 As a function of his paper quality, each author submits to a single journal, seeking to maximize caliber  $\times$  admission chance
  - ► Rational expectations: Acceptance decisions ensure that average acceptance quality equals advertised caliber



#### Model 1: The Author Knows His Paper Quality

- Continuum Mass of Authors
  - Each has a unique paper with some quality x
  - ▶ Density of paper qualities on  $[\underline{x}, \infty)$
- Continuum Mass of Journals
  - ▶ Journal *caliber* is the average quality of accepted papers
  - ► Caliber is \$\$ units: a caliber *v* publication is worth *v* to the author
  - Free entry / exit of journals of any caliber (endogenous players)
  - When journals have market power, this invalidates our competitive logic, and is an open problem.
- ► Information and Actions
  - ▶ Seeing his paper quality, an author picks a journal to submit to
  - Seeing a noisy evaluation signal  $\sigma$  of a submitted paper's quality, a journal chooses whether to accept or reject it
  - Location family noise: quality x paper yields realized signal  $\sigma$ , where  $\sigma x$  is atomless with a probability density g.
    - Example: Gaussian noise  $g(\sigma x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2\phi^2}(\sigma x)^2}$
    - Other distribution examples: (most) Gamma, exponential, extreme value, logistic, Weibull, and most beta distributions

#### A Robust Assumption on Signal Noise

- Information economics is prone to striking results that hold for one distribution and not others
  - e.g. main finding cascade finding of herding literature (9000+cites) depended on multinomial signals, and usually fails
  - ► The problem arises when you learn from people's actions
- lacksquare Signal density g is log-concave on  $[0,\infty)$  or  ${\mathbb R}$
- $\Rightarrow$  No signal is perfectly revealing
  - $\Rightarrow$  every paper has a positive chance at every journal
- ⇒ The density is positive on a connected interval
- ▶ Prekopa: signal cdf *G* is log-concave (and thus continuous)
- $\Rightarrow$  hazard rate  $\frac{g(t)}{1-G(t)}$  is increasing.

#### Journal Motivations

- Rational Expectations Equilibrium: promised caliber is realized
  - 1. Ours is an intuitive long-run steady-state journal reputation
  - 2. Bayesian persuasion sender-receiver story
    - Journals can publicly commit to acceptance standards
  - 3. Mercenary journal story:
    - ▶ Journal *profit* is average accepted paper quality minus caliber
    - Declining (eg predatory) journals reimburse authors for deficit between promised and delivered caliber
    - ▶ There is free entry of any journal that expects to earn profits
  - ▶ We use story 3 in order to quantity payoffs after deviations
- ▶ Journal v accepts when signal  $\sigma \ge \theta(v)$ , acceptance threshold
  - Accepting papers over the bar is optimal in the short run story

#### Author Payoffs

- Author's payoff is caliber times acceptance chance
  - We ignore journal application fees.
  - ▶ The opportunity cost (only one submission) is the critical one.
- Quality x paper submitted to a caliber v journal with threshold  $\theta$  pays

$$(1-G(\theta-x))\cdot v$$

- This subsumes dynamic case with resubmission and discounting when the author cares about  $(1 \delta)$  times this
  - Author resubmits to the same journal.

#### Distinct Papers are Sent to Distinct Journals in Equilibrium

#### Lemma

Every author submits to a journal equal to his caliber.

- Rational expectations  $\Rightarrow$  suffices to show that no journal  $v_1$  attracts paper qualities  $x < v_1$  and  $x' > v_1$
- If so, a new journal  $v_2 > v_1$  can skim off best papers at  $v_1$ 
  - Let the new journal promise higher caliber  $v_2 \in (v_1, x')$ , where x' is indifferent, given the acceptance thresholds  $\theta_1, \theta_2$ :

$$[1 - G(\theta_2 - x')]v_2 = [1 - G(\theta_1 - x')]v_1 \qquad (\diamondsuit)$$

Then journal  $v_2$  has higher standards than  $v_1$ . For logging  $(\diamondsuit)$ :  $\log(1-G(\theta_2-x'))-\log(1-G(\theta_1-x'))=\log(v_1/v_2)<0$ 

► Claim: (♣) has a unique solution 
$$\theta_2 > \theta_1$$

- ▶ Proof:  $\log[1 G]$  is concave  $\Rightarrow$  left side of (♣) continuously weakly falls in  $\theta_2$  from 0 at  $\theta_2 = \theta_1$ , tending to  $-\infty$  as  $\theta_2 \uparrow \infty$
- Next, all papers x'' > x' prefer journal  $v_2$ , and x'' < x' prefer  $v_1$ .
- ▶ Journal  $v_2$  attracts only papers  $x'' \ge x'$ , but promises caliber  $v_2 < x'$ . So it earns profits. Contradiction (given free entry).

#### Journal Equilibrium

▶ A journal equilibrium is an acceptance threshold function  $\theta(v)$  for which it is optimal for every author  $x \in [\underline{x}, \infty)$  to submit to the same caliber journal v = x

#### Proposition (A Unique Equilibrium Exists)

There exists a unique equilibrium.

Existence is an ODE result. More later...

#### The Worst Journal is not Selective

#### Lemma

The worst journal has caliber  $\underline{x}$ , and accepts all submissions.

▶ Proof: Since we ruled out pooling in equilibrium, the least caliber journal cannot exceed x

If the least journal  $\underline{x}$  sometimes rejects, a new journal can enter, always accept, and attract all paper qualities just over  $\underline{x} > 0$  (making profits). Contradiction.

Motivation

#### Equilibrium and Its First Order Condition

Author optimality, given paper of quality x:

$$\max_{v}(1-G(\theta(v)-x))v$$

Unlike with auctions, different authors have the same payoff from a given journal, but produce different signal distributions

#### Equilibrium and Its First Order Condition

Author optimality, given paper of quality x:

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- Unlike with auctions, different authors have the same payoff from a given journal, but produce different signal distributions
- ► FOC:

$$(1 - G(\theta(v) - x)) - g(\theta(v) - x)\theta'(v)v = 0$$

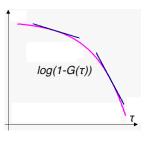
- ► The SOC holds, given log-concavity of G
- ightharpoonup By rational expectations, the FOC holds at quality x = v:

equilibrium FOC 
$$\Rightarrow$$
  $\theta'(v) = \frac{1}{v} \cdot \frac{1 - G(\theta(v) - v)}{g(\theta(v) - v)}$ 

▶ On the right side is the inverse hazard rate of evaluation noise:

#### Journal Rejection Rate is Hump-Shaped

- ightharpoonup toughness  $\tau(v) = \theta(v) v$
- We argue toughness is hump-shaped



acceptance rate 
$$\times$$
 caliber 
$$= [1 - G(\underbrace{\theta(v) - x}_{\text{toughness}})] \times v$$

- ▶ Optimality: 1% caliber rise is balanced by 1% acceptance fall
- ▶ Log-concavity: 1% falls in  $1 G \Rightarrow$  toughness % increases fall
- ▶ Eventually,  $\theta(v) \uparrow$  less % than caliber  $v \Rightarrow$  toughness falls

#### Proposition (Hump-Shaped Selectivity)

The equilibrium rejection rate  $R(v) = G(\tau(v))$  is hump-shaped in journal caliber v, for all small x > 0

Motivation

#### Proof of Hump-Shaped Journal Selectivity

Since  $\tau(v) = \theta(v) - v$ , we can rewrite equilibrium FOC as:

$$\tau'(v) = \theta'(v) - 1 = \frac{1}{v} \frac{1 - G(\tau(v))}{g(\tau(v))} - 1$$
 (\*)

- ▶ Idea:  $\tau(v)$  is hump-shaped, declining once  $\frac{g(\tau(v))}{1-G(\tau(v))} \ge \frac{1}{v}$
- lacktriangle Proof: By log-concavity, the hazard rate rises in au
  - $\Rightarrow$  If  $\tau(v)$  is weakly rising, then  $\tau'(v)$  is strictly falling, by  $(\bigstar)$
  - $\Rightarrow$  any critical point is a max:  $\tau'(v) = 0 \Rightarrow \tau''(v) < 0$ 
    - ▶ If  $\tau(v)$  rises forever, RHS of  $(\bigstar) \to -1 < 0$ . Contradiction!
- ▶ Finally,  $(\bigstar)$  implies that  $\tau'(\underline{x}) > 0$  for small enough  $\underline{x}$

#### Rejection Costs and Caliber

▶ How does *rejection cost*  $C(v) = G(\tau(v)) \cdot v$  vary in caliber?

#### Proposition

Rejection cost is hump-shaped in journal caliber v.

- ▶ Proof: Since toughness rises initially, so do rejection losses
- ▶ Rejection costs fall in *v* once

$$C'(v) = G(\tau(v)) + vg(\tau(v))\tau'(v) < 0 \qquad (5)$$

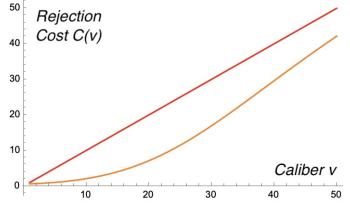
- ▶ Eq'm FOC (★) iff  $vg(\tau(v))\tau'(v) = 1 G(\tau(v)) vg(\tau(v))$ .
- $\Rightarrow$  Rejection losses fall ( $\ref{sol}$ ) iff  $vg(\tau(v)) > 1$ .
- ▶ We claim  $vg(\tau(v)) 1$  upcrosses (through 0)
- ▶ Given (★), when  $vg(\tau(v)) = 1$ , we have:

$$\frac{d}{dv}vg(\tau(v)) = g(\tau(v)) + vg'(\tau(v))\left(\frac{1 - G(\tau(v))}{vg(\tau(v))} - 1\right)$$
$$= g(\tau(v)) - G(\tau(v)g'(\tau(v))/g(\tau(v)) \ge 0$$

 $\triangleright$  ... by log concavity of G. Finally, losses do eventually fall!

#### Gaussian Example of Rejection Losses

As caliber v rises, rejection costs C(v) — the gap below initially rises and eventually falls



(Gaussian signals with variance 10)

#### Fully Solved Example with Exponential Referee Noise

•  $G(t) = 1 - e^{-\lambda t}$ : The equilibrium FOC at interior solution is:

$$\theta'(v) = \frac{1}{v} \cdot \left(\frac{1 - G(\theta(v) - v)}{g(\theta(v) - v)}\right) = \frac{1}{\lambda v} \Rightarrow \theta(v) = \frac{1}{\lambda} \log v + C$$

- ▶ Sure acceptance at journal  $\underline{x} \Rightarrow \theta(\underline{x}) = \underline{x}$  and  $C = \underline{x} \frac{1}{\lambda} \log \underline{x}$
- $\Rightarrow$  Acceptance threshold  $\theta(v) = \underline{x} + \frac{1}{\lambda} \log \frac{v}{\underline{x}}$  provided  $\theta(v) > v$ 
  - $\theta(v) = v \text{ at any journal } v > \overline{v}$
- $\Rightarrow$  Equilibrium rejection rate at interior solution at  $v < \bar{v}$  is

$$R(v) = G(\theta(v) - v) = 1 - e^{-\lambda(\theta(v) - v)} = 1 - \frac{X}{v}e^{\lambda(v - \underline{x})}$$

 $\Rightarrow$  Rejection cost at  $v < \bar{v}$ 

$$C(v) = vR(v) = v \left[1 - \frac{x}{v}e^{\lambda(v - \underline{x})}\right] = v - \underline{x}e^{\lambda(v - \underline{x})}$$

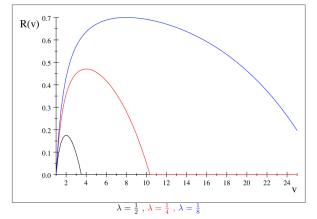
▶ Higher caliber journals  $v \ge \bar{v}$  accept everything at zero rejection cost

#### Fully Solved Example with Exponential Referee Noise

- ► Case 1: Precise signals:  $\lambda > 1/\underline{x}$ 
  - riangleright corner solution  $\theta(v) = v$ , and zero rejection chance in equilibrium for all paper qualities.
- ▶ Case 2: Noisy signals:  $\lambda < 1/\underline{x}$ 
  - ► A hump shape emerges
- low and high quality refereeing

#### Increasing Dispersion with Exponential Noise

#### As Signal Noise Rises, Rejection Rates Rise & Peak Later



Plots assume a worst paper  $\underline{x} = 1$ .

#### How Evaluation Noise Impacts Rejection Rates

- Dispersion measures how "spread out" a distribution is
- ▶ G is more dispersed than F  $\Leftrightarrow G^{-1}(b) - G^{-1}(a) \ge F^{-1}(b) - F^{-1}(a)$  for any b > a $\Leftrightarrow g(G^{-1}(a)) < f(F^{-1}(a))$  for any  $a \in (0,1)$ , with a density
- ► For many distributions, e.g. exponential and Gaussian, higher dispersion ← higher variance

#### Proposition (Increasing Dispersion)

The rejection rate rises and peaks later if G grows more disperse

► Low quality refereeing leads to higher rejection rates

# Motivation Authors Possible Occident

# Rejection Rate Rises in Evaluation Noise Dispersion

- ► Comparative statics for the rejection use operator methods
- ► Recall the equilibrium FOC

$$\theta'(v) = \frac{1 - G(\tau(v))}{vg(\tau(v))} \qquad (\bigstar)$$

▶ The *rejection rate*  $R(v) = G(\tau(v))$  has slope

$$R'(v) = g(\tau(v))\tau'(v)$$

$$= g(\tau(v))[\theta'(v) - 1]$$

$$= \frac{1 - R(v)}{v} - g(G^{-1}(R(v))) \qquad (\spadesuit)$$

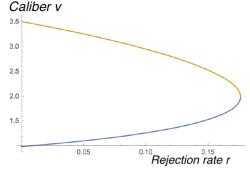
▶ The equilibrium rejection rate is a fixed point of the operator:

$$TR(v) = \int_0^v \left(\frac{1 - R(s)}{s} - g(G^{-1}(R(s)))\right) ds$$

- ► The *T* operator is neither a contraction nor monotone, but is a contraction on small enough intervals.
- ▶ We then paste together the unique fixed points

#### Comparative Statics via an Inverse Operator

- ▶ For comparative statics, invert R(v) to get V(r)
- As R(v) is hump-shaped, we invert its pre- and post-hump segments the blue curve  $V_L(r)$  and orange curve  $V_U(r)$



▶ By the Inverse Function Theorem and (♠), we have

$$V'_{L}(r) = \frac{1}{R'(V_{L}(r))} = \frac{V_{L}(r)}{1 - r - V_{L}(r) \cdot g(G^{-1}(r))}$$

#### Dispersion and the Lower Inverse

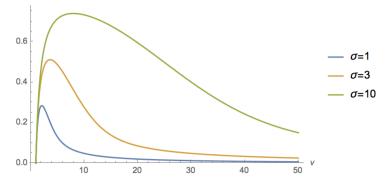
▶ The fixed point  $V_L(r)$  of  $\hat{T}$  obeys (since  $\underline{x} \equiv V(0)$ ):

$$\hat{T}V_L(r) = \underline{x} + \int_0^r \frac{V_L(s)}{1 - s - V_L(s) \cdot g(G^{-1}(s))} ds$$

- ▶ If G grows more dispersed, the function  $g(G^{-1}(s))$  falls
  - $\Rightarrow$  The operator  $\hat{\mathcal{T}}$  shifts down
  - $\Rightarrow$  Its fixed point  $V_L$  shifts down
  - $\Rightarrow$  Also, orange curve  $V_U$  shifts up, meeting  $V_L$  at a higher v
  - $\Rightarrow$  Its inverse, the rejection rate R(v), shifts up (and peaks later)

### Rejection Rates with Noisier Gaussian Signals

► As Signal Noise Rises, Rejection Rates Rise & Peak Later



#### What if Authors Do Not Know Paper Quality?

- Authors may be unsure of their paper's quality just as a student may not know how good he is
- Our results should still inform what happens in the stage game, but authors would learn over time

▶ But authors exploit optionality & submit more ambitiously



#### The Full Model with Incomplete Information

- lacktriangle Journal sees signal  $\sigma$  of paper quality x of any submission
  - $ightharpoonup \sigma x$  has a density  $g(\sigma x)$
- lacktriangle Author sees a noisy signal  $\psi$  of the quality x of his paper,
  - $\psi x$  has a density  $h(\psi x)$ .
- ▶ Paper quality density f is log-concave on  $[\underline{x}, \infty)$  (say  $\underline{x} = 1$ )
  - Until now, the paper quality distribution was irrelevant for the conclusion, for neither authors nor journals needed Bayes rule
- ► We seek a pure strategy Bayes Nash equilibrium with
  - ightharpoonup higher author types  $\psi$  apply more ambitiously
  - ► higher journal types set higher standards
- ightharpoonup A separating equilibrium is  $(V, \theta)$ , i.e. a smoothly increasing
  - (a) application function  $V(\psi)$  yielding author optimality, and
  - (b) acceptance threshold  $\theta(v)$  yielding rational expectations.

#### Journal Equilibrium

- Inverting  $V(\psi)$ : author signal  $\Psi(v)$  submits to caliber v
- ► The density of accepted paper qualities x at journal v:

Authors Know Paper Quality

$$\alpha(x|v) \propto f(x)h(\Psi(v)-x)(1-G(\theta(v)-x))$$

► The *rational expectations* (RE) condition reflects that journals now publish a variety of qualities:

$$\mathsf{RE} \qquad \mathsf{v} = \int_{\mathsf{x}}^{\infty} \mathsf{x} \alpha(\mathsf{x}|\mathsf{v}) \mathsf{d}\mathsf{x}$$

**b** journal equilibrium  $(\Psi, \theta)$  obeys RE & author optimality:

FOC\* 
$$\frac{1}{v\theta'(v)} = \int_{x}^{\infty} \frac{g(\theta(v) - x)}{1 - G(\theta(v) - x)} \alpha(x|v) dx$$

► The integrals reflects how authors don't know their quality *x*, and so journals cannot infer them from application

#### Equilibrium Rejection Rate

▶ The density of submitted paper qualities x at journal  $\theta$ 

$$\zeta(x|v) \propto f(x)h(\Psi(v)-x)$$

► The equilibrium *rejection rate* is now

$$R(v) = \int_{\underline{x}}^{\infty} \zeta(x|v) G(\theta(v) - x) dx$$

- Higher-caliber journals
  - use higher acceptance thresholds  $(\theta \uparrow)$ , rejecting any given quality x paper with larger chance  $G(\theta(v) x) \uparrow$
  - **P** get submissions from higher author signals  $(\Psi \uparrow)$ , with a higher paper density  $\zeta$  (stochastically), clearing the bar more often
- ► The rejection rate is hump-shaped if the first effect dominates at low calibers, the second effect at high calibers

#### Journal Equilibrium Equations, Reformulated

- equilibrium toughness  $\tau(v) \equiv \theta(v) v$  is again the excess of the journal threshold over its caliber
- **▶** author's equilibrium sheepishness  $\xi(v) \equiv \Psi(v) v$  is the excess of the author's type over journal caliber
- ▶ Define *caliber-quality gap*  $z \equiv v x$ 
  - lacktriangle the accepted-paper-quality density  $lpha_{m{
    u}}$  is

$$\alpha(\mathbf{v}-\mathbf{z}|\mathbf{v}) \propto f(\mathbf{v}-\mathbf{z})h(\xi(\mathbf{v})+\mathbf{z})(1-G(\tau(\mathbf{v})+\mathbf{z}))$$

- f log-concave iff f(v-z) is logsupermodular (LSPM) in (v,z)
- So  $\alpha$  is LSPM in (v, z) if sheepishness  $\xi(v)$  is decreasing

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- ▶ So  $\alpha$  is LSPM in (v, z) if sheepishness  $\xi(v)$  is decreasing
- ▶ Rewrite equilibrium equations (replacing  $\theta(v)$  by  $\tau(v) + v$ ) as:

FOC\* 
$$\frac{1}{v\theta'(v)} = \int_{-\infty}^{v-1} \alpha(v-z|v) \frac{g(\tau(v)+z)}{1-G(\tau(v)+z)} dz$$
RE  $0 = \int_{-\infty}^{v-1} \alpha(v-z|v) z dz$ 

- ► Rational expectations: the average caliber-quality gap is zero
- sheepishness  $\xi$  decreasing function  $\Rightarrow \alpha$  LSPM  $\Rightarrow$  expected caliber-quality gap is positive  $\Rightarrow$  RE fails

#### Questions

1. Equilibrium toughness  $\tau(v)$  hump-shaped?

2. Hump-shaped toughness  $\Rightarrow$  hump-shaped rejection rates?

### Quasiconcave Toughness is Tough

- We prove that any critical point  $\tau'(v) = 0$  is a max, i.e. that  $\tau'(v) = \theta'(v) 1$  downcrosses through zero
- ▶ i.e. when  $\tau'(v) = 0$ , the following FOC\* formula rises in v:

$$1/\theta'(v) = v \cdot \int_{-\infty}^{v-1} \alpha(v-z|v) \frac{g(\tau(v)+z)}{1-G(\tau(v)+z)}$$

- ▶ This would be easy if  $\alpha(v z|v)$  were LSPM in (v, z), since:
  - lacktriangle the hazard rate g/(1-G) increases with z by log-concavity
  - by monotonicity preservation, its mean rises given a LSPM kernel increases with v (Milgrom's (1981) "Good News")
- ▶ But then  $\int \alpha(v-z|v)zdz$  also increases, violating RE
- Likewise,  $\alpha(v z|v)$  cannot shift upward in FOSD in v (weaker than LSPM)

#### Decreasingly Log-concave Distributions

 $\blacktriangleright$  We posit f, h are decreasingly log-concave:

$$(\log f)'', (\log h)'' \le 0 \le (\log f)''', (\log h)'''$$

- Examples include most log-concave densities: Gaussian, exponential, uniform, Chi-squared, extreme value, etc.
- Let cdf A(z|v) have density  $\alpha(v-z|v)$  in z
- ▶ Decreasingly log concave  $\Rightarrow -\frac{\partial}{\partial v}A(z|v)$  is *upcrossing* through zero in z (rather than everywhere positive, as FOSD yields)
- ▶ RE holds: increasing  $v \Rightarrow$  mean-preserving spread in A(z|v)
- ► First case: convex hazard rates (e.g. Gaussian)
  - ► Mean-preserving spread raises mean of a convex hazard rate.
  - ▶ So when  $\tau'(v) = 0$ , the following rises in v

$$1/\theta'(v) = v \cdot \int_{-\infty}^{v-1} \alpha(v - z|v) \frac{g(\tau(v) + z)}{1 - G(\tau(v) + z)}$$

► This proves quasiconcavity of toughness

#### Quasiconcave Toughness

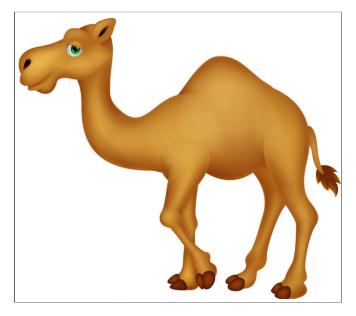
- We exploit richer properties to sweep in other distributions
- ▶ Does quasiconcave toughness ⇒ hump-shaped toughness?
- ► Hump-shaped toughness ⇒ hump-shaped rejection rates?
- With known author types, hump-shaped toughness was necessary and sufficient for a hump-shaped rejection curve, via

$$R(v) \equiv G(\tau(v))$$

#### Lemma

Equilibrium toughness is hump-shaped if author information is not too dispersed, and otherwise increasing

## When do Humps Emerge



#### Main Findings

#### Result 1

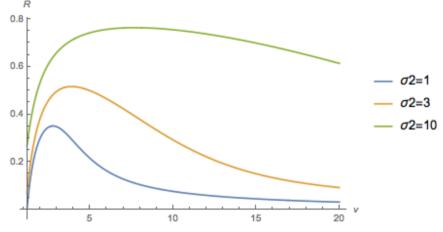
If the author signal is sufficiently less noisy than the journal signal, then the rejection rate R(v) is hump-shaped; otherwise, it is everywhere increasing.

#### Result 2

The rejection rate rises as the journal OR author signal noise increases.

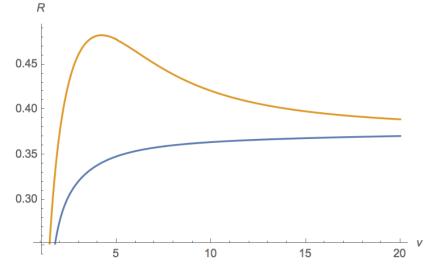
#### Gaussian Location Signals for Author and Journal

As journal signal noise rises, rejection rates rise & peak later



Assume an improper uniform prior f, standard normal author signal distribution, and journal signal as above.

# Humps Emerge with More Precise Author Information



- ▶ both use paper prior  $f = \Gamma[2, 1]$ , author signal  $h = \Gamma[2, 1]$
- ▶ journal signals  $g = \Gamma[2,1]$  (blue) and  $g = \Gamma[2,2]$  (orange)

# Mavi's Sheep



#### Journal Rejection Rates

Hamermesh (2008), "How to Publish in a Top Journal"

- ▶ QJE 4%, JPE 5%, AER 7%, APSR 8%, JoLE 8%
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- ► RAND 11%, REStat 12%, Economics Letters 17%
- ► Canadian Journal of Economics 18%
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Authors Know Paper Quality	When Authors Don't Know their Paper Quality
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Massachusetts Institute of Technology	MA	8
University of Chicago	IL	8
Brown University	RI	9
University of Pennsylvania	PA	9